

$$\begin{aligned} \text{d) } \log \left( x^4 \cdot \sqrt[3]{\frac{4x}{(y-x)^2}} \right) &= \log \left( x^4 \cdot \left( \frac{4x}{(y-x)^2} \right)^{\frac{1}{3}} \right) = \log x^4 + \frac{1}{3} \cdot \log \left( \frac{4x}{(y-x)^2} \right) = \\ &= 4 \log x + \frac{1}{3} \cdot (\log 4x - \log (y-x)^2) = 4 \log x + \frac{1}{3} \cdot (\log 4 + \log x - 2 \cdot \log(y-x)) = \\ &= 4 \log x + \frac{1}{3} \log 4 + \frac{1}{3} \log x - \frac{2}{3} \log(y-x) = \frac{13}{3} \log x + \frac{1}{3} \log 4 - \frac{2}{3} \log(y-x) \end{aligned}$$