

LÖSUNG ZU 281:

$$f(x) = ax^4 + bx^3 + cx^2 + dx + e$$

$$f'(x) = 4ax^3 + 3bx^2 + 2cx + d$$

$$f''(x) = 12ax^2 + 6bx + 2c$$

$$f''(0) = 0 \quad \text{Wendepunkt}$$

$$f'(0) = 0 \quad \text{da } t: y = 1 \quad (\text{k ist also } 0)$$

$$f(0) = 1 \quad \text{da } y = 1$$

$$f(2) = -7 \quad \text{Punkt auf Funktion}$$

$$f'(2) = 0 \quad \text{Tiefpunkt}$$

$$f''(0) = 0 \quad \rightarrow \quad c = 0$$

$$f'(0) = 0 \quad \rightarrow \quad d = 0$$

$$f(0) = 1 \quad \rightarrow \quad e = 1$$

$$f'(2) = 0 \quad \begin{array}{l} 0 = 32a + 12b \\ 0 = 4 \cdot (8a + 3b) \quad / : 4 \end{array}$$

$$0 = 8a + 3b \quad / - 3b$$

$$-3b = 8a \quad / : 8$$

$$\frac{-3b}{8} = a$$

$$f(2) = -7 = 16a + 8b + 1 \quad \frac{-3b}{8} = a$$

$$-7 = \frac{-3b}{8} \cdot 16 + 8b + 1$$

$$-7 = -6b + 8b + 1$$

$$-7 = 2b + 1 \quad / - 1$$

$$-8 = 2b$$

$$b = -4 \quad \rightarrow \quad a = \frac{-3 \cdot (-4)}{8} = \frac{12}{8} = 1,5$$

$$f(x) = 1,5x^4 - 4x^3 + 1$$

